Fall 2020	ENG 5300	Test 1	Chris Collins
You must show all	work to receive full credit.	All work is to be your	<mark>r own.</mark> Oct 19 2020
This is a closed boo	oks and notes test. Be orga	anized. Total point	ts: 100 18:40-19:55
Submit to BB a single b/w pdf file, named using your last name. emailed solutions won't be graded			
1. §10.1 Line Inte	egral. Work done by a forc	e. Calculate $\int_C \mathbf{F}(\mathbf{r})$	$d \mathbf{r}$ for the following data. If \mathbf{F} is a
force, this gives the work done in the displacement along C . (Show the details.)			

 $\mathbf{F} = [x, -z, 2y], \text{, from } (1, 2, 3) \text{ straight to } (3, 2, 1).$ 10 points

2. §10.2 Check for Path Independence and, if independent, integrate from (0, 0, 0) to (a, b, c). (Show the details of your work.) 10 points

$$xy z^2 dx + \frac{1}{2}x^2 z^2 dy + x^2 yz dz$$

3. §10.4 Evaluation of Line Integrals by Green's Theorem. Using Green's Theorem, evaluate $\oint_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r}$ counterclockwise around the boundary curve C of the region R, where $\mathbf{F} = [\cosh y, -\sinh x], R: 1 \le x \le 3, x \le y \le 3x$ 20 points 4. §10.6 Flux Integrals (3) $\iint_{S} \mathbf{F} \cdot \mathbf{n} \, dA$ Evaluate the integral for the given data. Describe the kind of surface. Show the details of your work. 20 points $\mathbf{F} = [e^y, e^x, 1], S: x + y + z = 1, x \ge 0, y \ge 0, z \ge 0$

5. §10.7 Application of the Divergence Theorem: Surface Integrals $\oiint {\bf F}\cdot {\bf n}\, dA$

20 points

Evaluate the integral by the Divergence Theorem. (Show the details.) $\mathbf{F} = [5x^3, 5y^3, 5z^3], S: x^2 + y^2 + z^2 = 4$ *Hint*: The following facts might be useful:

Cartesian coordinates: $dV = dx \, dy \, dz$

Cylindrical coordinates: $dV = r \, dr \, d\theta \, dz$, $0 \le \theta \le 2\pi$, $r \ge 0$, $x = r \cos \theta$, $y = r \sin \theta$, z = zSpherical coordinates: $dV = \rho^2 \sin \phi \, d\rho \, d\phi \, d\theta$, $0 \le \theta \le 2\pi$, $0 \le \phi \le \pi$, $\rho \ge 0$, $x = \rho \sin \phi \cos \theta$, $y = \rho \sin \phi \sin \theta$, $z = \rho \cos \phi$ 6. §10.9 Evaluation of $\oint_C \mathbf{F} \cdot \mathbf{r}' \, ds$

20 points

Calculate this line integral by Stokes's theorem for the given \mathbf{F} and C. Assume the Cartesian coordinates to be right-handed and the z-component of the surface normal to be nonnegative. Show the details.

 $\mathbf{F} = [e^y, 0, e^x], C$ around the triangle with vertices (0, 0, 0), (1, 0, 0), (1, 1, 0)