

You must show **all** work to receive full credit. All work is to be your own.

Oct 19 2020

This is a closed books and notes test. Be organized. Total points: **100**

**18:40- 19:55**

Submit to BB a single b/w pdf file, named using your last name. emailed solutions won't be graded

1. §10.1 Line Integral. Work done by a force. Calculate  $\int_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r}$  for the following data. If  $\mathbf{F}$  is a force, this gives the work done in the displacement along  $C$ . (Show the details.)  
 $\mathbf{F} = [x - y, y - z, z - x]$ ,  $C : \mathbf{r} = [2 \cos t, t, 2 \sin t]$  from  $(2, 0, 0)$  to  $(2, 2\pi, 0)$ . 10 points

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2. §10.2 Check for Path Independence and, if independent, integrate from  $(0, 0, 0)$  to  $(a, b, c)$ .  
(Show the details of your work.) 10 points

$$e^y dx + (xe^y - e^z) dy - ye^z dz$$

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3. §10.4 Evaluation of Line Integrals by Green's Theorem. Using Green's Theorem, evaluate  $\oint_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r}$  counterclockwise around the boundary curve  $C$  of the region  $R$ , where  $\mathbf{F} = [x \cosh 2y, 2x^2 \sinh 2y]$ ,  $R: x^2 \leq y \leq x$ . 20 points

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4. §10.6 Flux Integrals (3)  $\iint_S \mathbf{F} \cdot \mathbf{n} dA$  Evaluate the integral for the given data. Describe the kind of surface. Show the details of your work. 20 points
- $\mathbf{F} = [y^2, x^2, z^4]$ ,  $S : z = 4\sqrt{x^2 + y^2}$ ,  $0 \leq z \leq 8$ ,  $y \geq 0$

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5. §10.7 Application of the Divergence Theorem: Surface Integrals  $\iint_S \mathbf{F} \cdot \mathbf{n} \, dA$

20 points

Evaluate the surface integral  $\iint_S \mathbf{F} \cdot \mathbf{n} \, dA$  by the Divergence Theorem. Show the details.

$\mathbf{F} = [x^3 - y^3, y^3 - z^3, z^3 - x^3]$ ,  $S$ , the surface of  $x^2 + y^2 + z^2 \leq 25$ ,  $z \geq 0$

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6. §10.9 Evaluation of  $\oint_C \mathbf{F} \cdot \mathbf{r}' ds$

20 points

Calculate this line integral by Stokes's theorem for the given  $\mathbf{F}$  and  $C$ . Assume the Cartesian coordinates to be right-handed and the  $z$ -component of the surface normal to be nonnegative. Show the details.

$\mathbf{F} = [y^2, x^2, z + x]$ , around the triangle with vertices  $(0, 0, 0)$ ,  $(1, 0, 0)$ ,  $(1, 1, 0)$