

You must show **all** work to receive full credit. All work is to be your own.

Oct 19 2020

This is a closed books and notes test. Be organized. Total points: **100**

**18:40- 19:55**

Submit to BB a single b/w pdf file, named using your last name. emailed solutions won't be graded

1. §10.1 Line Integral. Work done by a force. Calculate  $\int_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r}$  for the following data. If  $\mathbf{F}$  is a force, this gives the work done in the displacement along  $C$ . (Show the details.)  
 $\mathbf{F} = [z, x, y]$ ,  $C : \mathbf{r} = [\cos t, \sin t, t]$  from  $(1, 0, 0)$  to  $(1, 0, 4\pi)$ . 10 points

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2. §10.2 Check for Path Independence and, if independent, integrate from  $(0, 0, 0)$  to  $(a, b, c)$ .  
(Show the details of your work.) 10 points

$$(\cos(x^2 + 2y^2 + z^2))(2x dx + 4y dy + 2z dz)$$

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3. §10.4 Evaluation of Line Integrals by Green's Theorem. Using Green's Theorem, evaluate  $\int_C \mathbf{F}(\mathbf{r}) \cdot d\mathbf{r}$  counterclockwise around the boundary curve  $C$  of the region  $R$ , where  $\mathbf{F} = [x^2 + y^2, x^2 - y^2]$ ,  $R : 1 \leq y \leq 2 - x^2$ . Sketch  $R$ . 20 points

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4. §10.6 Flux Integrals (3)  $\iint_S \mathbf{F} \cdot \mathbf{n} \, dA$  Evaluate the integral given below for the following data.

Indicate the kind of surface. (Show the details of your work.)

20 points

$\mathbf{F} = [\tan xy, x, y]$ ,  $S : y^2 + z^2 = 1$ ,  $2 \leq x \leq 5$ ,  $y \geq 0$ ,  $z \geq 0$

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5. §10.7 Application of the Divergence Theorem: Surface Integrals  $\iint_S \mathbf{F} \cdot \mathbf{n} \, dA$

20 points

Evaluate the integral by the Divergence Theorem. (Show the details.)

$$\mathbf{F} = [z - y, y^3, 2z^3], \quad S \text{ the surface of } y^2 + z^2 \leq 4, -3 \leq x \leq 3$$

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6. §10.9 Evaluation of  $\oint_C \mathbf{F} \cdot \mathbf{r}' ds$

20 points

Calculate this line integral by Stokes's theorem for the given  $\mathbf{F}$  and  $C$ . Assume the Cartesian coordinates to be right-handed and the  $z$ -component of the surface normal to be nonnegative. Show the details.

$\mathbf{F} = [0, z^3, 0]$ ,  $C$  the boundary curve of the cylinder  $x^2 + y^2 = 1$ ,  $x \geq 0$ ,  $y \geq 0$ ,  $0 \leq z \leq 1$